Closing Tues: 13.1 Closing Thur: 13.2, 13.3 Closing *next* Tues: 13.4 Exam 1 is next Tues, Oct. 23 covers 12.1-12.6, 13.1-13.4 2D Examples Eliminate the parameters 1. $x = t, y = 2 - t^2$

13.1: Intro to 3D Vector Curves

To visualize 3D-curves, we start by Step 1: Find surface/path of motion. Step 2: Plot points.

2.
$$x = 3\cos(4t)$$
, $y = 4\sin(4t)$

3D Example x = t, y = cos(2t), z = sin(2t) *Example:* All pts given by the equations

the Now plot points!

x = t, $y = \cos(2t)$, $z = \sin(2t)$ are on the cylinder: $y^2 + z^2 = 1$.



Another 3D Examples $x = t \cos(t), y = t \sin(t), z = t$ *Example:* All pts given by the equations

 $x = t \cos(t), y = t \sin(t), z = t$

are on the cone $z^2 = x^2 + y^2$.





Now plot points!

Intersection issues

For all intersection questions, combine the conditions

(a) Intersecting a curve and surface.

Combine conditions

Example:

Find all intersections of

 $x = t, y = \cos(\pi t), z = \sin(\pi t)$ with the surface

$$x^2 - y^2 - z^2 = 3.$$



(b) Intersecting two curves.

Use two different parameters!!! Combine conditions.

We say the objects **collide** if the intersection happens at the same parameter value (i.e. same time).

Example:

Two particles are moving according to

 $r_1(t) = \langle t, 5t, 9 \rangle$, and $r_2(t) = \langle t - 2, 5, t^2 \rangle$.

Do their paths intersect? Do they collide?

(c) *Intersecting two surfaces*.

Answer will be a 3D curve. To parameterize the curve:

Let one variable be *t*. Solve for others in terms of *t*.

OR For circle/ellipse try

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \Leftrightarrow \begin{array}{l} x = a \cos(t) \\ y = b \sin(t) \end{array}$$

Examples

1. Find *any* parametric equations that describe the curve of intersection of $z = 2x + y^2$ and z = 2y 2. Find *any* parametric equations that describe the curve of intersection of $x^2 + y^2 = 1$ and z = 5 - x $x^2 + y^2 = 1$ and $z^2 = x^2 + y^2$

